

# Synchronization in networks with multiple interaction layers

## Supplementary Material

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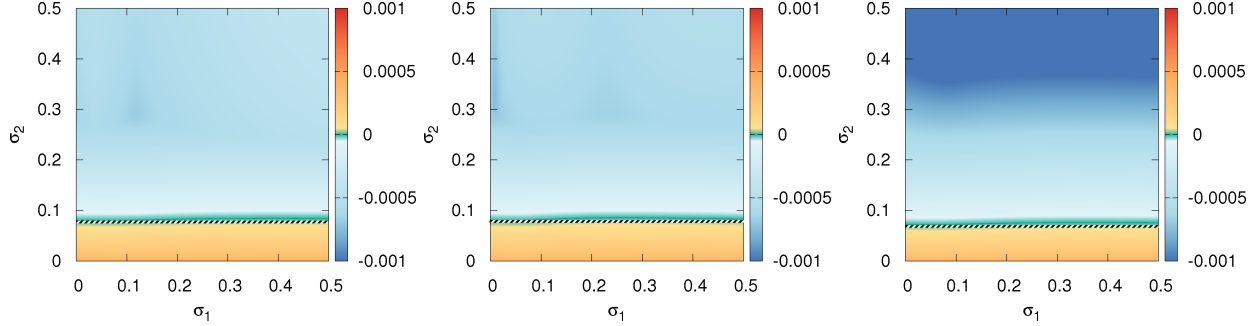


Figure S1: Maximum Lyapunov exponent  $\Lambda$  for systems falling into Case 1 (layer 1 in stability class I, layer 2 in stability class II), for SF-SF, ER-SF and SF-ER topologies (left panel, centre panel and right panel, respectively). The dark blue lines mark the points in the  $(\sigma_1, \sigma_2)$  space where  $\Lambda$  vanishes, while the striped lines indicate the critical value of  $\sigma_2$  if layer 2 is considered in isolation (or, equivalently, if  $\sigma_1 = 0$ ).

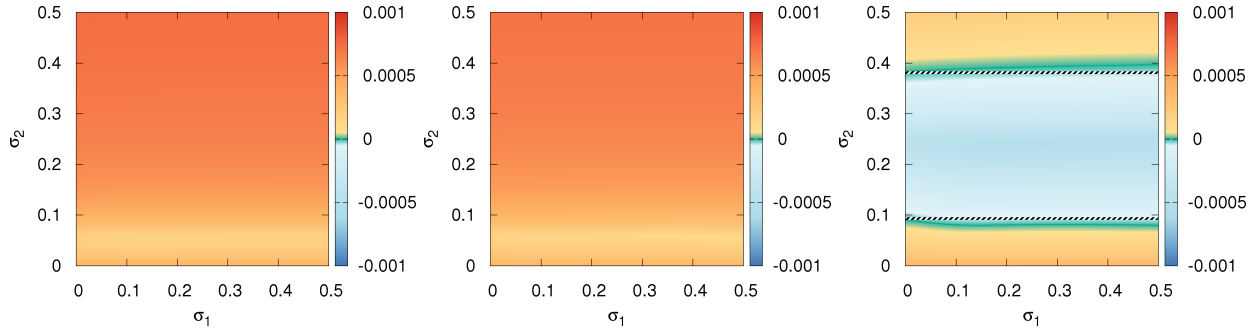


Figure S2: Maximum Lyapunov exponent  $\Lambda$  for systems falling into Case 2 (layer 1 in stability class I, layer 2 in stability class III), for SF-SF, ER-SF and SF-ER topologies (left panel, centre panel and right panel, respectively). The dark blue lines mark the points in the  $(\sigma_1, \sigma_2)$  space where  $\Lambda$  vanishes, while the striped lines indicate the critical values of  $\sigma_2$  if layer 2 is considered in isolation (or, equivalently, if  $\sigma_1 = 0$ ).

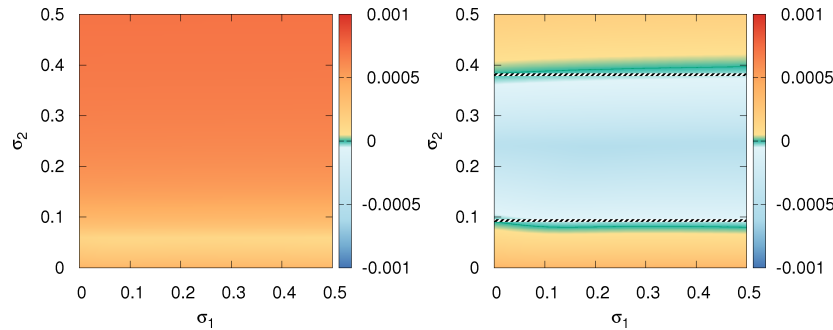


Figure S3: Maximum Lyapunov exponent  $\Lambda$  for systems falling into Case 3 (layer 1 in stability class II, layer 2 in stability class III), for ER-SF and SF-ER topologies (left panel and right panel, respectively). The dark blue lines mark the points in the  $(\sigma_1, \sigma_2)$  space where  $\Lambda$  vanishes, while the striped lines indicate the stability limits for the  $\sigma_1 = 0$  and  $\sigma_2 = 0$ .